



#### ABOUT EUREKA MATH

Created by the nonprofit Great Minds, *Eureka Math* helps teachers deliver unparalleled math instruction that provides students with a deep understanding and fluency in math. Crafted by teachers and math scholars, the curriculum carefully sequences the mathematical progressions to maximize coherence from Prekindergarten through Precalculus—a principle tested and proven to be essential in students' mastery of math.

Teachers and students using *Eureka Math* find the trademark "Aha!" moments in *Eureka Math* to be a source of joy and inspiration, lesson after lesson, year after year.

# **ALIGNED**

Eureka Math is the only curriculum found by EdReports.org to align fully with the Common Core State Standards for Mathematics for all grades, Kindergarten through Grade 8. Great Minds offers detailed analyses which demonstrate how each grade of Eureka Math aligns with specific state standards. Access these free alignment studies at greatminds.org/state-studies.

## DATA

Schools and districts nationwide are experiencing student growth and impressive test scores after using *Eureka Math*. See their stories and data at greatminds.org/data.

# FULL SUITE OF RESOURCES

As a nonprofit, Great Minds offers the *Eureka Math* curriculum as PDF downloads for free, noncommercial use. Access the free PDFs at greatminds.org/math/curriculum.

The teacher—writers who created the curriculum have also developed essential resources, available only from Great Minds, including the following:

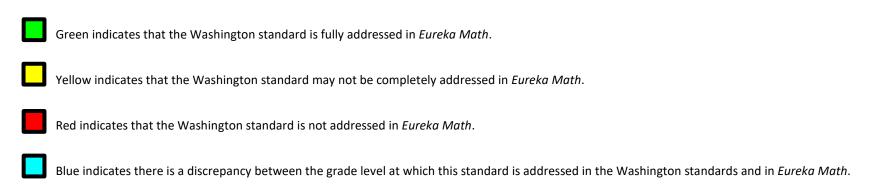
- Printed material in English and Spanish
- Digital resources
- Professional development
- · Classroom tools and manipulatives
- Teacher support materials
- Parent resources

# Mississippi College- and Career-Readiness Standards for Mathematics Correlation to *Eureka Math* TM

# **ALGEBRA II**

The majority of the Algebra II Mississippi College- and Career- Readiness Standards for Mathematics are fully covered by the Algebra II *Eureka Math*™ curriculum. The areas where the Algebra II Mississippi College- and Career- Readiness Standards for Mathematics and Algebra II *Eureka Math* do not align will require the use of *Eureka Math* content from other courses. A detailed analysis of alignment is provided in the table below.

# **INDICATORS**



# Aligned Components of Eureka Math

## 1: Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

Lessons in every module engage students in making sense of problems and persevering in solving them as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 1, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

# Aligned Components of Eureka Math

# 2: Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents—and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

Lessons in every module engage students in reasoning abstractly and quantitatively as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 2, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

# Aligned Components of Eureka Math

3: Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

Lessons in every module engage students in constructing viable arguments and critiquing the reasoning of others as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 3, which is specifically addressed in the following modules:

Algebra II M2: Trigonometric Functions

# Aligned Components of Eureka Math

#### 4: Model with mathematics.

Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

Lessons in every module engage students in modeling with mathematics as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 4, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

# Aligned Components of Eureka Math

## 5: Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

Lessons in every module engage students in using appropriate tools strategically as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 5, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M4: Inferences and Conclusions from Data

# 6: Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

Lessons in every module engage students in attending to precision as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 6, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

# Aligned Components of Eureka Math

#### 7: Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see  $7 \times 8$  equals the well remembered  $7 \times 5 + 7 \times 3$ , in preparation for learning about the distributive property. In the expression  $x^2 + 9x + 14$ , older students can see the 14 as  $2 \times 7$  and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see  $5 - 3(x - y)^2$  as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.

Lessons in every module engage students in looking for and making use of structure as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 7, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

# 8: Look for and express regularity in repeated reasoning.

Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through (1, 2) with slope 3, middle school students might abstract the equation (y-2)/(x-1)=3. Noticing the regularity in the way terms cancel when expanding (x-1)(x+1),  $(x-1)(x^2+x+1)$ , and  $(x-1)(x^3+x^2+x+1)$  might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

Lessons in every module engage students in looking for and expressing regularity in repeated reasoning as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 8, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
Number and	The Real	Cluster: Extend the properties of exponents to ra	tional exponents
Quantity	Number System (N-RN)	<b>N-RN.1</b> Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. For example, we define 51/3 to be the cube root of 5 because we want [51/3]3 = 5(1/3) 3 to hold, so [51/3]3 must equal 5.	Algebra II M3 Topic A: Real Numbers
		N-RN.2 Rewrite expressions involving radicals and rational exponents using the properties of exponents.	Algebra II M3 Topic A: Real Numbers
	Quantities (N-Q) *	Cluster: Reason quantitatively and use units to solve problems	
		N-Q.2 Define appropriate quantities for the purpose of descriptive modeling. *	Algebra I M1 Topic A: Introduction to Functions Studied this Year—Graphing Stories  Algebra I M5: A Synthesis of Modeling with Equations and Functions
	The Complex	Cluster: Perform arithmetic operations with complex numbers.	
	Number System (N-CN)	<b>N-CN.1</b> Know there is a complex number $i$ such that $i^2 = -1$ , and every complex number has the form $a + bi$ with $a$ and $b$ real.	Algebra II M1 Lesson 37: A Surprising Boost from Geometry

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		<b>N-CN.2</b> Use the relation $i^2 = -1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.	Algebra II M1 Lesson 37: A Surprising Boost from Geometry
		Cluster: Use complex numbers in polynomial ide	ntities and equations.
		N-CN.7 Solve quadratic equations with real coefficients that have complex solutions.	Algebra II M1 Lesson 38: Complex Numbers as Solutions to Equations  Algebra II M1 Lesson 39: Factoring Extended to the Complex Realm
Algebra	Seeing Structure in	Cluster: Interpret the structure of expressions.	
	Expressions	A-SSE.2 Use the structure of an expression to identify ways to rewrite it.	Algebra II M1 Topic A: Polynomials—From Base Ten to Base X  Algebra II M1 Lesson 12: Overcoming Obstacles in Factoring  Algebra II M1 Lesson 13: Mastering Factoring  Algebra II M3 Lesson 12: Properties of Logarithms  Algebra II M3 Lesson 14: Solving Logarithmic Equations  Algebra II M3 Lesson 15: Why Were Logarithms Developed?

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Write expressions in equivalent forms to	solve problems.
		A-SSE.3  Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. *  c. Use the properties of exponents to transform expressions for exponential functions. For example, the expression 1.15t can be rewritten as [1.15 <sup>1/12</sup> ] <sup>12t</sup> += 1.012 <sup>12t</sup> to reveal the approximate equivalent monthly interest rate if the annual rate is 15%.	Algebra I M3 Lesson 23: Newton's Law of Cooling  Algebra II M3 Lesson 26: Percent Rate of Change
		A-SSE.4  Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems.	Algebra II M3 Topic E: Geometric Series and Finance
	Arithmetic with Polynomials and Rational Expressions (A-APR)	Cluster: Understand the relationship between zeros and factors of polynomials.	
		<b>A-APR.2</b> Know and apply the Remainder Theorem: For a polynomial $p(x)$ and a number $a$ , the remainder on division by $x - a$ is $p(a)$ , so $p(a) = 0$ if and only if $(x - a)$ is a factor of $p(x)$ .	Algebra II M1 Lesson 19: The Remainder Theorem

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		<b>A-APR.3</b> Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial. (Limit to 1 <sup>st</sup> - and 2 <sup>nd</sup> - degree polynomials).	Algebra II M1 Lesson 11: The Special Role of Zero in Factoring  Algebra II M1 Lesson 14: Graphing Factored Polynomials
		Cluster: Use polynomial identities to solve proble	ems.
		A-APR.4 Prove polynomial identities and use them to describe numerical relationships.	Algebra II M1 Topic A: Polynomials—From Base Ten to Base X
		Cluster: Rewrite rational expressions.	
		<b>A-APR.6</b> Rewrite simple rational expressions in different forms; write $a(x)/b(x)$ in the form $q(x) + r(x)/b(x)$ , where $a(x)$ , $b(x)$ , $q(x)$ , and $r(x)$ are polynomials with the degree of $r(x)$ less than the degree of $b(x)$ , using inspection, long division, or, for the more complicated examples, a computer algebra system.	Algebra II M1 Lesson 4: Comparing Methods—Long Division, Again?  Algebra II M1 Lesson 18: Overcoming a Second Obstacle in Factoring—What If There Is a Remainder?  Algebra II M1 Lesson 22: Equivalent Rational Expressions  Algebra II M1 Lesson 24: Multiplying and Dividing Rational Expressions  Algebra II M1 Lesson 25: Adding and Subtracting Rational Expressions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
	Creating Equations (A-	Cluster: Create equations that describe numbers	or relationships.
	CED) *	A-CED.1 Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. *	Algebra II M1 Lesson 27: Word Problems Leading to Rational Equations  Algebra II M3 Lesson 7: Bacteria and Exponential Growth  Algebra II M3 Lesson 26: Percent Rate of Change  Algebra II M3 Lesson 27: Modeling with Exponential Functions
		A-CED.2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. [Note this Standard appears in previous courses with a slight variation in the standard language.]	Algebra II M1 Lesson 1: Successive Differences in Polynomials  Algebra II M1 Lessons 16–17: Modeling with Polynomials—An Introduction  Algebra II M1 Lessons 20–21: Modeling Riverbeds with Polynomials  Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior  Algebra II M2 Lesson 13: Tides, Sound Waves, and Stock Markets
		A-CED.3 Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.	Algebra II M1 Lessons 20–21: Modeling Riverbeds with Polynomials Algebra II M3 Topic E: Geometric Series and Finance

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
	Reasoning with	Cluster: Understand solving equations as a process of reasoning and explain the reasoning.	
	Equations and Inequalities (A-REI.1  Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.  A-REI.2  Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.  Cluster: Solve equations and inequalities in one variables.	Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify	Algebra I M1 Lesson 12: Solving Equations  Algebra I M1 Lesson 13: Some Potential Dangers when Solving Equations  Algebra I M1 Lesson 17: Equations Involving Factored Expressions  Algebra I M1 Lesson 18: Equations Involving a Variable Expression in the Denominator
		Solve simple rational and radical equations in one variable, and give examples showing how	Algebra II M1 Lesson 22: Equivalent Rational Expressions Algebra II M1 Lesson 23: Comparing Rational Expressions Algebra II M1 Lesson 26: Solving Rational Equations Algebra II M1 Lesson 27: Word Problems Leading to Rational Equations Algebra II M1 Lesson 28: A Focus on Square Roots Algebra II M1 Lesson 29: Solving Radical Equations
		variable.	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		A-REI.4  Solve quadratic equations in one variable. b. Solve quadratic equations by inspection (e.g., for x² = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions.	Algebra I M4 Lesson 5: The Zero Product Property  Algebra I M4 Lesson 6: Solving Basic One-Variable Quadratic Equations  Algebra I M4 Lesson 7: Creating and Solving Quadratic Equations in One Variable  Algebra I M4 Lesson 13: Solving Quadratic Equations by Completing the Square  Algebra I M4 Lesson 14: Deriving the Quadratic Formula  Algebra I M4 Lesson 15: Using the Quadratic Formula  Algebra II M1 Lesson 31: Systems of Equations  Algebra II M1 Lesson 38: Complex Numbers as Solutions to Equations
		Cluster: Solve systems of equations	
		A-REI.6 Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.	Algebra I M1 Lessons 22-23: Solution Sets to Simultaneous Equations  Algebra I M1 Lesson 24: Applications of Systems of Equations and Inequalities  Algebra I M4 Lesson 24: Modeling with Quadratic Functions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		A-REI.7 Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. For example, find the points of intersection between the line $y = -3x$ and the circle $x^2 + y^2 = 3$ .	Algebra II M1 Lesson 31: Systems of Equations  Algebra II M1 Lesson 32: Graphing Systems of Equations
		Cluster: Represent and solve equations and inequ	ualities graphically.
		A-REI.11 Explain why the $x$ -coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$ ; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions. *	Algebra I M3 Lesson 16: Graphs Can Solve Equations Too Algebra II M1 Lesson 36: Overcoming a Third Obstacle to Factoring—What If There Are No Real Number Solutions? Algebra II M3 Lesson 24: Solving Exponential Equations
Functions	Interpreting	Cluster: Understand the concept of a function an	d use function notation.
	Functions (F-IF)	<b>F-IF.3</b> Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers.	Algebra I M3 Lesson 2: Recursive Formulas for Sequences Algebra I M3 Lesson 3: Arithmetic and Geometric Sequences Algebra I M3 Lesson 4: Why Do Banks Pay YOU to Provide Their Services?

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
		Cluster: Interpret functions that arise in applications in terms of the context.		
		F-IF.4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. *	Algebra II M1 Lessons 16–17: Modeling with Polynomials—An Introduction  Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior  Algebra II M2 Lesson 13: Tides, Sound Waves, and Stock Markets  Algebra II M3 Lesson 18: Graphs of Exponential Functions and Logarithmic Functions  Algebra II M3 Lesson 20: Transformations of the Graphs of Logarithmic and Exponential Functions  Algebra II M3 Lesson 21: The Graph of the Natural Logarithm Function	
		F-IF.6 Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. *	Algebra II M3 Lesson 6: Euler's Number, e Algebra II M3 Lesson 27: Modeling with Exponential Functions	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
		Cluster: Analyze functions using different representations.		
		<b>F-IF.7</b> Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.		
		Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior.	Algebra II M1 Lesson 14: Graphing Factored Polynomials  Algebra II M1 Lesson 15: Structure in Graphs of Polynomial Functions  Algebra II M1 Lesson 16: Modeling with Polynomials—An Introduction	
		e. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.	Algebra II M2 Lesson 8: Graphing the Sine and Cosine Functions  Algebra II M2 Lesson 11: Transforming the Graph of the Sine Function  Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior  Algebra II M3 Lesson 16: Rational and Irrational Numbers  Algebra II M3 Lesson 18: Graphs of Exponential Functions and Logarithmic Functions  Algebra II M3 Lesson 20: Transformations of the Graphs of Logarithmic and Exponential Functions  Algebra II M3 Lesson 33: The Million Dollar Problem	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		F-IF.8 Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. b. Use the properties of exponents to interpret expressions for exponential functions.	Algebra II M3 Lesson 23: Bean Counting  Algebra II M3 Lesson 27: Modeling with Exponential Functions  Algebra II M3 Topic E: Geometric Series and Finance
		F-IF.9  Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.	Algebra II M3 Lesson 27: Modeling with Exponential Functions  Algebra II M3 Lesson 28: Newton's Law of Cooling, Revisited  Algebra II M3 Topic E: Geometric Series and Finance
	Building Functions (F- BF)	Cluster: Build a function that models a relationsh	nip between two quantities.
		<b>F-BF.1</b> Write a function that describes a relationship between two quantities.	
		Determine an explicit expression, a recursive process, or steps for calculation from a context.	Algebra I M3: Linear and Exponential Functions  Algebra I M5: A Synthesis of Modeling with Equations and Functions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		b. Combine standard function types using arithmetic operations.	Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior  Algebra II M3 Lesson 28: Newton's Law of Cooling, Revisited  Algebra II M3 Lesson 30: Buying a Car  Algebra II M3 Lesson 33: The Million Dollar Problem
		F-BF.2 Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms. *	Algebra I M3 Topic A: Linear and Exponential Sequences  Algebra II M3 Lesson 25: Geometric Sequences and Exponential Growth and Decay  Algebra II M3 Lesson 26: Percent Rate of Change
		Cluster: Build new functions from existing function	ons.
		<b>F-BF.3</b> Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$ , $k$ $f(x)$ , $f(kx)$ , and $f(x + k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. <i>Include recognizing even and odd functions from their graphs and algebraic expressions for them.</i>	Algebra II M1 Lesson 15: Structure in Graphs of Polynomial Functions  Algebra II M2 Lesson 11: Transforming the Graph of the Sine Function  Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior  Algebra II M3 Lesson 20: Transformations of the Graphs of Logarithmic and Exponential Functions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		<ul> <li>F-BF.4</li> <li>Find inverse functions.</li> <li>a. Solve an equation of the form f(x) = c for a simple function f that has an inverse and write an expression for the inverse.</li> </ul>	Algebra II M3 Lesson 7: Bacteria and Exponential Growth Algebra II M3 Lesson 8: The "WhatPower" Function Algebra II M3 Lesson 19: The Inverse Relationship Between Logarithmic and Exponential Functions Algebra II M3 Lesson 24: Solving Exponential Equations
	Linear,	Cluster: Construct and compare linear, quadratic, and exponential models and solve problems.	
	Quadratic, and Exponential Models (F-LE) *	F-LE.2 Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table). *	Algebra I M3: Linear and Exponential Functions  Algebra I M5: A Synthesis of Modeling with Equations and Functions  Algebra II M3 Lesson 1: Integer Exponents
		F-LE.3  Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly quadratically, or (more generally) as a polynomial function. *	Algebra I M3 Lesson 5: The Power of Exponential Growth  Algebra I M3 Lesson 6: Exponential Growth—U.S. Population and World Population  Algebra I M3 Lesson 14: Linear and Exponential Models— Comparing Growth Rates  Algebra I M3 Lesson 21: Comparing Linear and Exponential Models Again

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		<b>F-LE.4</b> For exponential models, express as a logarithm the solution to $ab^{ct} = d$ where $a$ , $c$ , and $d$ are numbers and the base $b$ is 2, 10, or $e$ ; evaluate the logarithm using technology.	Algebra II M3 Topic B: Logarithms  Algebra II M3 Lesson 19: The Inverse Relationship Between Logarithmic and Exponential Functions  Algebra II M3 Topic D: Using Logarithms in Modeling Situations
		Cluster: Interpret expressions for functions in ter	rms of the situation they model.
		F-LE.5 Interpret the parameters in a linear or exponential function in terms of a context. *	Algebra I M3 Topic D: Using Functions and Graphs to Solve Problems
	Trigonometric Functions	Cluster: Extend the domain of trigonometric functions using the unit circle.	
		<b>F-TF.1</b> Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle.	Algebra II M2 Lesson 9: Awkward! Who Chose the Number 360, Anyway?
		F-TF.2 Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle.	Algebra II M2: Trigonometric Functions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
Geometry	Expressing Geometric Properties with Equations (G- GPE)	Cluster: Translate between the geometric description and the equation for a conic section	
		<b>G-GPE.2</b> Derive the equation of a parabola given a focus and directrix.	Algebra II M1 Lesson 33: The Definition of a Parabola Algebra II M1 Lesson 34: Are All Parabolas Congruent? Algebra II M1 Lesson 35: Are All Parabolas Similar?
Statistics and Interpreting		Cluster: Summarize, represent, and interpret data on a single count or measurement variable.	
Probability	Categorical and Quantitative Data (S-ID)	S-ID.4  Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use calculators, spreadsheets, and tables to estimate areas under the normal curve. *	Algebra II M4 Topic B: Modeling Data Distributions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Summarize, represent, and interpret data on two categorical and quantitative variables.	
		S-ID.6 Represent data on two quantitative variables on a scatter plot, and describe how the variables are related. *  a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.	Algebra I M2 Lessons 12–13: Relationships Between Two Numerical Variables  Algebra I M2 Lesson 19: Interpreting Correlation  Algebra I M2 Lesson 20: Analyzing Data Collected on Two Variables  Algebra I M5 Lesson 7: Modeling a Context from Data
	Making	Cluster: Understand and evaluate random processes underlying statistical experiments.	
	Inferences and Justifying Conclusions (S- IC)	S-IC.1 Understand statistics as a process for making	Algebra II M4 Topic C: Drawing Conclusions Using Data from a Sample
	ic)	inferences about population parameters based on a random sample from that population. *	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Make inferences and justify conclusions from sample surveys, experiments, and observational studies.	
		S-IC.3  Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each. *	Algebra II M4 Lesson 12: Types of Statistical Studies  Algebra II M4 Topic D: Drawing Conclusions Using Data from an Experiment
		S-IC.4 Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling. *	Algebra II M4 Topic C: Drawing Conclusions Using Data from a Sample
		S-IC.5 Use data from a randomized experiment to compare two treatments; use simulations to decide if differences between parameters are significant. *	Algebra II M4 Topic D: Drawing Conclusions Using Data from an Experiment

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		S-IC.6 Evaluate reports based on data. *	Algebra II M4 Lesson 22: Evaluating Reports Based on Data from a Sample  Algebra II M4 Topic D: Drawing Conclusions Using Data from an Experiment
	Conditional		
		Cluster: Use probability to evaluate outcomes of	decisions.
	Conditional Probability and the Rules of Probability (S- CP)	Cluster: Use probability to evaluate outcomes of  S-CP.1  Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or," "and," "not"). *	decisions.  Algebra II M4 Topic A: Probability

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		S-CP.3 Understand the conditional probability of $A$ given $B$ as $P(A \text{ and } B)/P(B)$ , and interpret independence of $A$ and $B$ as saying that the conditional probability of $A$ given $B$ is the same as the probability of $A$ , and the conditional probability of $B$ given $A$ is the same as the probability of $B$ . *	Algebra II M4 Lesson 4: Calculating Conditional Probabilities and Evaluating Independence Using Two-Way Tables  Algebra II M4 Lesson 6: Probability Rules
		S-CP.4 Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. For example, collect data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results. *	Algebra II M4 Lesson 2: Calculating Probabilities of Events Using Two-Way Tables  Algebra II M4 Lessons 3–4: Calculating Conditional Probabilities and Evaluating Independence Using Two-Way Tables
		S-CP.5 Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations. For example, compare the chance of having lung cancer if you are a smoker with the chance of being a smoker if you have lung cancer. *	Algebra II M4 Topic A: Probability

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Use the rules of probability to compute prodel	probabilities of compound events in a uniform probability
		S-CP.6 Find the conditional probability of A given B as the fraction of B's outcomes that also belong to A, and interpret the answer in terms of the model. *	Algebra II M4 Lessons 3–4: Calculating Conditional Probabilities and Evaluating Independence Using Two-Way Tables
		S-CP.7 Apply the Addition Rule, $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ , and interpret the answer in terms of the model.*	Algebra II M4 Lesson 7: Probability Rules

<sup>\*</sup> Modeling Standards