EUREKA MATH[™]

ABOUT EUREKA MATH	Created by the nonprofit Great Minds, <i>Eureka Math</i> helps teachers deliver unparalleled math instruction that provides students with a deep understanding and fluency in math. Crafted by teachers and math scholars, the curriculum carefully sequences the mathematical progressions to maximize coherence from Prekindergarten through Precalculus—a principle tested and proven to be essential in students' mastery of math.		
	Teachers and students using <i>Eureka Math</i> find the trademark "Aha!" moments in <i>Eureka Math</i> to be a source of joy and inspiration, lesson after lesson, year after year.		
ALIGNED	<i>Eureka Math</i> is the only curriculum found by EdReports.org to align fully with the Common Core State Standards for Mathematics for all grades, Kindergarten through Grade 8. Great Minds offers detailed analyses which demonstrate how each grade of <i>Eureka Math</i> aligns with specific state standards. Access these free alignment studies at greatminds.org/state-studies.		
DATA	Schools and districts nationwide are experiencing student growth and impressive test scores after using <i>Eureka Math</i> . See their stories and data at greatminds.org/data.		
FULL SUITE OF RESOURCES	As a nonprofit, Great Minds offers the <i>Eureka Math</i> curriculum as PDF downloads for free, noncommercial use. Access the free PDFs at greatminds.org/math/curriculum.		
	The teacher–writers who created the curriculum have also developed essential resources, available only from Great Minds, including the following:		
	 Printed material in English and Spanish Digital resources Professional development Classroom tools and manipulatives 		
	Teacher support materials		

• Parent resources

<u>ALGEBRA II</u>

The majority of the Algebra II Tennessee State Mathematics Standards are fully covered by the Algebra II *Eureka Math* curriculum. The areas where the Algebra II Tennessee State Mathematics Standards and Algebra II *Eureka Math* do not align will require the use of *Eureka Math* content from another course. A detailed analysis of alignment is provided in the table below.

INDICATORS

Green indicates that the Tennessee standard is fully addressed in *Eureka Math*.

Yellow indicates that the Tennessee standard may not be completely addressed in *Eureka Math*.

Red indicates that the Tennessee standard is not addressed in *Eureka Math*.

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Blue indicates there is a discrepancy between the grade level at which this standard is addressed in the Tennessee standards and in Eureka Math.
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1: Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

Lessons in every module engage students in making sense of problems and persevering in solving them as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 1, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

2: Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to *decontextualize*—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents and the ability to *contextualize*, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand, considering the units involved, attending to the meaning of quantities, not just how to compute them, and knowing and flexibly using different properties of operations and objects. Lessons in every module engage students in reasoning abstractly and quantitatively as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 2, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

3: Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and, if there is a flaw in an argument, explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

Lessons in every module engage students in constructing viable arguments and critiquing the reasoning of others as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 3, which is specifically addressed in the following modules:

Algebra II M2: Trigonometric Functions

4: Model with mathematics.

Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts, and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

Lessons in every module engage students in modeling with mathematics as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 4, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

5: Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a compass, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

Lessons in every module engage students in using appropriate tools strategically as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 5, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

6: Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, expressing numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school, they have learned to examine claims and make explicit use of definitions. Lessons in every module engage students in attending to precision as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 6, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

7: Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see 7×8 equals the well-remembered $7 \times 5 + 7 \times 3$, in preparation for learning about the distributive property. In the expression $x^2 + 9x + 14$, older students can see the 14 as 2×7 and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see $5-3(x-y)^2$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers *x* and *y*.

Lessons in every module engage students in looking for and making use of structure as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 7, which is specifically addressed in the following modules:

Algebra II M1: Polynomial, Rational, and Radical Relationships

Algebra II M2: Trigonometric Functions

Algebra II M3: Exponential and Logarithmic Functions

8: Look for and express regularity in repeated reasoning. Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through $(1, 2)$ with slope 3, middle school students might abstract the equation $(y - 2)/(x - 1) = 3$. Noticing the regularity in the way terms cancel when expanding $(x - 1)(x + 1), (x - 1)(x^2 + x + 1), \text{ and } (x - 1)(x^3 + x^2 + x + 1)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.	 Lessons in every module engage students in looking for and expressing regularity in repeated reasoning as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 8, which is specifically addressed in the following modules: Algebra II M1: Polynomial, Rational, and Radical Relationships Algebra II M2: Trigonometric Functions Algebra II M3: Exponential and Logarithmic Functions
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Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
Number	The Real	Cluster: Extend the properties of	exponents to rational exponents.	
and Quantity	Number System	A2.N.RN.A.1	Algebra II M3 Topic A: Real Numbers	
		Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents.		
		A2.N.RN.A.2	Algebra II M3 Topic A: Real Numbers	
		Rewrite expressions involving radicals and rational exponents using the properties of exponents.		
	Quantities	Cluster: Reason quantitatively and use units to solve problems.		
		A2.N.Q.A.1 Identify, interpret, and justify	Algebra I M1 Topic A: Introduction to Functions Studied this Year—Graphing Stories	
	appropriate quantities for the purpose of descriptive modeling.	Algebra I M5: A Synthesis of Modeling with Equations and Functions		
			Algebra II M1 Lessons 20–21: Modeling Riverbeds with Polynomials	
			Algebra II M3 Lesson 2: Base 10 and Scientific Notation	
			Algebra II M3 Lesson 9: Logarithms—How Many Digits Do You Need?	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
	The Complex	Cluster: Perform arithmetic oper	rations with complex numbers.
	Number System	A2.N.CN.A.1 Know there is a complex number <i>i</i> such that $i^2 = -1$, and every complex number has the form $a + bi$ with a and b real.	Algebra II M1 Lesson 37: A Surprising Boost from Geometry
		A2.N.CN.A.2 Know and use the relation $i^2 = -1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.	Algebra II M1 Lesson 37: A Surprising Boost from Geometry
		Cluster: Use complex numbers in	quadratic equations.
		A2.N.CN.B.3 Solve quadratic equations with real coefficients that have complex solutions.	Algebra II M1 Lesson 38: Complex Numbers as Solutions to Equations
			Algebra II M1 Lesson 39: Factoring Extended to the Complex Realm

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
Algebra	Seeing	Cluster: Interpret the structure	of expressions.
	Structure in Expressions	A2.A.SSE.A.1 Use the structure of an expression to identify ways to rewrite it.	 Algebra II M1 Topic A: Polynomials—From Base Ten to Base X Algebra II M1 Lesson 12: Overcoming Obstacles in Factoring Algebra II M1 Lesson 13: Mastering Factoring Algebra II M3 Lesson 12: Properties of Logarithms Algebra II M3 Lesson 14: Solving Logarithmic Equations Algebra II M3 Lesson 15: Why Were Logarithms Developed?

Conceptual Category	Domain	Standards for Mathematical Content		Aligned Components of Eureka Math
		Cluster: Use expressions in equi	iva	lent forms to solve problems.
		A2.A.SSE.B.2 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.		
		a. Use the properties of exponents to rewrite expressions for exponential functions.		Algebra II M3 Lesson 23: Bean Counting Algebra II M3 Lesson 27: Modeling with Exponential Functions Algebra II M3 Topic E: Geometric Series and Finance
		A2.A.SSE.B.3 Recognize a finite geometric series (when the common ratio is not 1), and know and use the sum formula to solve problems in context.		Algebra II M3 Topic E: Geometric Series and Finance

Conceptual Category	Domain	Standards for Mathematical Content		Aligned Components of Eureka Math
	Arithmetic	Cluster: Understand the relation	sh	nip between zeros and factors of polynomials.
	with Polynomials and Rational Expressions	A2.A.APR.A.1 Know and apply the Remainder Theorem: For a polynomial $p(x)$ and a number a , the remainder on division by $x - a$ is $p(a)$, so p(a) = 0 if and only if $(x - a)$ is a factor of $p(x)$.		Algebra II M1 Lesson 19: The Remainder Theorem
		A2.A.APR.A.2 Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.		Algebra II M1 Lesson 11: The Special Role of Zero in Factoring Algebra II M1 Lesson 14: Graphing Factored Polynomials
		Cluster: Use polynomial identitie	es	to solve problems.
		A2.A.APR.B.3 Know and use polynomial identities to describe numerical relationships.		Algebra II M1 Topic A: Polynomials—From Base Ten to Base X

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Rewrite rational express	sions.
		A2.A.APR.C.4 Rewrite rational expressions in different forms.	 Algebra II M1 Lesson 4: Comparing Methods—Long Division, Again? Algebra II M1 Lesson 18: Overcoming a Second Obstacle in Factoring—What If There Is a Remainder? Algebra II M1 Lesson 22: Equivalent Rational Expressions Algebra II M1 Lesson 24: Multiplying and Dividing Rational Expressions Algebra II M1 Lesson 25: Adding and Subtracting Rational Expressions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
	Creating	Cluster: Create equations that de	escribe numbers or relationships.
	Equations	A2.A.CED.A.1 Create equations and inequalities in one variable and use them to solve problems.	Algebra II M1 Lesson 27: Word Problems Leading to Rational EquationsAlgebra II M3 Lesson 7: Bacteria and Exponential GrowthAlgebra II M3 Lesson 26: Percent Rate of ChangeAlgebra II M3 Lesson 27: Modeling with Exponential Functions
		A2.A.CED.A.2 Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.	Algebra I M1 Lesson 19: Rearranging Formulas

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
	Reasoning with	Cluster: Understand solving equa reasoning.	Cluster: Understand solving equations as a process of reasoning and explain the reasoning.	
	Equations and Inequalities	A2.A.REI.A.1 Explain each step in solving an equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.	 Algebra I M1 Lesson 12: Solving Equations Algebra I M1 Lesson 13: Some Potential Dangers when Solving Equations Algebra I M1 Lesson 17: Equations Involving Factored Expressions Algebra I M1 Lesson 18: Equations Involving a Variable Expression in the Denominator Algebra II M1 Lesson 28: A Focus on Square Roots 	
		A2.A.REI.A.2 Solve rational and radical equations in one variable, and identify extraneous solutions when they exist.	Algebra II M1 Lesson 22: Equivalent Rational ExpressionsAlgebra II M1 Lesson 23: Comparing Rational ExpressionsAlgebra II M1 Lesson 23: Comparing Rational ExpressionsAlgebra II M1 Lesson 26: Solving Rational EquationsAlgebra II M1 Lesson 27: Word Problems Leading to Rational EquationsAlgebra II M1 Lesson 28: A Focus on Square Roots Algebra II M1 Lesson 29: Solving Radical Equations	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Solve equations and inec	qualities in one variable.
		A2.A.REI.B.3 Solve quadratic equations and inequalities in one variable.	
		a. Solve quadratic equations by inspection (e.g., for $x^2 = 49$), taking square roots, completing the square, knowing and applying the quadratic formula, and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm bi$ for real numbers a and b .	 Algebra I M4 Lesson 5: The Zero Product Property Algebra I M4 Lesson 6: Solving Basic One-Variable Quadratic Equations Algebra I M4 Lesson 7: Creating and Solving Quadratic Equations in One Variable Algebra I M4 Lesson 14: Deriving the Quadratic Formula Algebra I M4 Lesson 15: Using the Quadratic Formula Algebra II M1 Lesson 31: Systems of Equations Algebra II M1 Lesson 38: Complex Numbers as Solutions to Equations

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math		
		Cluster: Solve systems of equation	ons.		
		A2.A.REI.C.4 Write and solve a system of linear equations in context.	 Algebra I M1 Lessons 22–23: Solution Sets to Simultaneous Equations Algebra I M1 Lesson 24: Applications of Systems of Equations and Inequalities Algebra I M4 Lesson 24: Modeling with Quadratic Functions 		
		A2.A.REI.C.5 Solve a system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically.	 Algebra II M1 Lesson 31: Systems of Equations Algebra II M1 Lesson 32: Graphing Systems of Equations Algebra II M1 Lesson 36: Overcoming a Third Obstacle to Factoring—What If There Are No Real Number Solutions? 		
		Cluster: Represent and solve equations graphically.			
		A2.A.REI.D.6 Explain why the <i>x</i> -coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$; find the approximate solutions using technology.	 Algebra I M3 Lesson 16: Graphs Can Solve Equations Too Algebra II M1 Lesson 36: Overcoming a Third Obstacle to Factoring—What If There Are No Real Number Solutions? Algebra II M3 Lesson 24: Solving Exponential Equations 		

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
Functions	Interpreting	Cluster: Interpret functions that	arise in applications in terms of the context.
	Functions	A2.F.IF.A.1 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship.	 Algebra II M1 Lessons 16–17: Modeling with Polynomials—An Introduction Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior Algebra II M2 Lesson 13: Tides, Sound Waves, and Stock Markets Algebra II M3 Lesson 18: Graphs of Exponential Functions and Logarithmic Functions Algebra II M3 Lesson 20: Transformations of the Graphs of Logarithmic and Exponential Functions Algebra II M3 Lesson 21: The Graph of the Natural Logarithm Function
		A2.F.IF.A.2 Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.	Algebra II M3 Lesson 6: Euler's Number, <i>e</i> Algebra II M3 Lesson 27: Modeling with Exponential Functions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Analyze functions using	different representations.
		A2.F.IF.B.3	
		Graph functions expressed symbolically and show key features of the graph, by hand and using technology.	
		a. Graph square root, cube root, and piecewise defined functions, including step functions and absolute value functions.	 Algebra I M3 Topic C: Transformations of Functions Algebra I M4 Lesson 18: Graphing Cubic, Square Root, and Cube Root Functions Algebra I M4 Lesson 19: Translating Graphs of Functions Algebra I M4 Lesson 20: Stretching and Shrinking Graphs of Functions
		b. Graph polynomial functions, identifying zeros when suitable factorizations are available and showing end behavior.	Algebra II M1 Lesson 14: Graphing Factored Polynomials Algebra II M1 Lesson 15: Structure in Graphs of Polynomial Functions Algebra II M1 Lesson 16: Modeling with Polynomials— An Introduction

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		c. Graph exponential and logarithmic functions, showing intercepts and end behavior.	 Algebra II M3 Lesson 16: Rational and Irrational Numbers Algebra II M3 Lesson 18: Graphs of Exponential Functions and Logarithmic Functions Algebra II M3 Lesson 20: Transformations of the Graphs of Logarithmic and Exponential Functions Algebra II M3 Lesson 33: The Million Dollar Problem
		A2.F.IF.B.4 Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.	
		a. Know and use the properties of exponents to interpret expressions for exponential functions.	Algebra II M3 Lesson 23: Bean Counting Algebra II M3 Lesson 27: Modeling with Exponential Functions Algebra II M3 Topic E: Geometric Series and Finance

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		A2.F.IF.B.5 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).	Algebra II M3 Lesson 27: Modeling with Exponential Functions Algebra II M3 Lesson 28: Newton's Law of Cooling, Revisited Algebra II M3 Topic E: Geometric Series and Finance
	Building Functions	Cluster: Build a function that mo	dels a relationship between two quantities.
		A2.F.BF.A.1 Write a function that describes a relationship between two quantities.	
		a. Determine an explicit expression, a recursive process, or steps for calculation from a context.	 Algebra II M1 Lesson 1: Successive Differences in Polynomials Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior Algebra II M3 Lesson 5: Irrational Exponents—What are 2^{√2} and 2^π? Algebra II M3 Lesson 6: Euler's Number, <i>e</i> Algebra II M3 Lesson 7: Bacteria and Exponential Growth Algebra II M3 Lesson 26: Percent Rate of Change Algebra II M3 Lesson 27: Modeling with Exponential Functions

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		b. Combine standard function types using arithmetic operations.	 Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior Algebra II M3 Lesson 28: Newton's Law of Cooling, Revisited Algebra II M3 Lesson 30: Buying a Car Algebra II M3 Lesson 33: The Million Dollar Problem
		A2.F.BF.A.2 Know and write arithmetic and geometric sequences with an explicit formula and use them to model situations.	 Algebra I M3 Topic A: Linear and Exponential Sequences Algebra II M3 Lesson 25: Geometric Sequences and Exponential Growth and Decay Algebra II M3 Lesson 26: Percent Rate of Change Algebra II M3 Lesson 29: The Mathematics Behind a Structured Savings Plan

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Build new functions from	n existing functions.
		A2.F.BF.B.3 Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, f(kx), and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology.	 Algebra II M2 Lesson 11: Transforming the Graph of the Sine Function Algebra II M2 Lesson 12: Ferris Wheels—Using Trigonometric Functions to Model Cyclical Behavior Algebra II M3 Lesson 20: Transformations of the Graphs of Logarithmic and Exponential Functions
		A2.F.BF.B.4 Find inverse functions.	
		a. Find the inverse of a function when the given function is one-to-one.	Algebra II M3 Lesson 7: Bacteria and Exponential Growth Algebra II M3 Lesson 8: The "WhatPower" Function
			Algebra II M3 Lesson 19: The Inverse Relationship Between Logarithmic and Exponential Functions
			Algebra II M3 Lesson 24: Solving Exponential Equations

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
	Linear, Quadratic,	Cluster: Construct and compare linear, quadratic, and exponential models and solve problems.		
	Quadratic, and Exponential Models	A2.F.LE.A.1 Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a table, a description of a relationship, or input-output pairs.	 Algebra II M1 Lesson 1: Successive Differences in Polynomials Algebra II M3 Lesson 6: Euler's Number, <i>e</i> Algebra II M3 Lesson 25: Geometric Sequences and Exponential Growth and Decay Algebra II M3 Lesson 26: Percent Rate of Change Algebra II M3 Topic E: Geometric Series and Finance 	
		A2.F.LE.A.2 For exponential models, express as a logarithm the solution to $ab^{ct} = d$ where <i>a</i> , <i>c</i> , and <i>d</i> are numbers and the base <i>b</i> is 2, 10, or <i>e</i> ; evaluate the logarithm using technology.	Algebra II M3 Topic B: LogarithmsAlgebra II M3 Lesson 19: The Inverse Relationship Between Logarithmic and Exponential FunctionsAlgebra II M3 Topic D: Using Logarithms in Modeling Situations	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Interpret expressions fo	or functions in terms of the situation they model.
		A2.F.LE.B.3 Interpret the parameters in a linear	Algebra I M3 Topic D: Using Functions and Graphs to Solve Problems
		or exponential function in terms of a context.	Algebra II M3 Lesson 23: Bean Counting
			Algebra II M3 Topic E: Geometric Series and Finance
	Trigonometric	Cluster: Extend the domain of tri	igonometric functions using the unit circle.
	Functions	A2.F.TF.A.1	
		Understand and use radian measure of an angle.	
		a. Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle.	Algebra II M2 Lesson 9: Awkward! Who Chose the Number 360, Anyway?
		b. Use the unit circle to find $sin(\theta)$, $cos(\theta)$, or $tan(\theta)$ when	Algebra II M2 Lesson 4: From Circle-ometry to Trigonometry
		θ is a commonly recognized angle between 0 and 2π .	Algebra II M2 Lesson 5: Extending the Domain of Sine and Cosine to All Real Numbers
			Algebra II M2 Lesson 6: Why Call It Tangent?
			Algebra II M2 Lesson 10: Basic Trigonometric Identities from Graphs

Conceptual Category	Domain	Standards for Mathematical Content		Aligned Components of Eureka Math
		A2.F.TF.A.2 Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle.		Algebra II M2: Trigonometric Functions
		Cluster: Prove and apply trigono)m	netric identities.
		A2.F.TF.B.3 Know and use trigonometric identities to find values of trig functions.		
		a. Given a point on a circle centered at the origin, recognize and use the right triangle ratio definitions of $sin(\theta)$, $cos(\theta)$, and $tan(\theta)$ to evaluate the trigonometric functions.		Algebra II M2 Lesson 4: From Circle-ometry to Trigonometry Algebra II M2 Lesson 5: Extending the Domain of Sine and Cosine to All Real Numbers Algebra II M2 Lesson 6: Why Call It Tangent? Algebra II M2 Lesson 10: Basic Trigonometric Identities from Graphs

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
		b. Given the quadrant of the angle, use the identity $\sin^2(\theta) + \cos^2(\theta) = 1$ to find $\sin(\theta)$ given $\cos(\theta)$, or vice versa.	Algebra II M2 Lesson 15: What Is a Trigonometric Identity?	
Statistics and	Interpreting Categorical and	Cluster: Summarize, represent, a measurement variable.	and interpret data on a single count or	
Probability	and Quantitative Data	A2.S.ID.A.1 Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages using the Empirical Rule.	Algebra II M4 Topic B: Modeling Data Distributions	
		Cluster: Summarize, represent, and interpret data on two categorical and quantitative variables.		
		A2.S.ID.B.2 Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.		
		a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data.	Algebra II M1 Lessons 20–21: Modeling Riverbeds with Polynomials Algebra II M2 Lesson 13: Tides, Sound Waves, and Stock Markets	

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
	Making Inferences	Cluster: Make inferences and jus and observational studies.	tify conclusions from sample surveys, experiments,
	and Justifying Conclusions Conditional Probability	A2.S.IC.A.1 Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each.	Algebra II M4 Lesson 12: Types of Statistical Studies Algebra II M4 Topic D: Drawing Conclusions Using Data from an Experiment
		A2.S.IC.A.2 Use data from a sample survey to estimate a population mean or proportion; use a given margin of error to solve a problem in context.	Algebra II M4 Topic C: Drawing Conclusions Using Data from a Sample
		Cluster: Understand independen interpret data.	ce and conditional probability and use them to
	and the Rules of Probability	A2.S.CP.A.1 Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or," "and," "not").	Algebra II M4 Topic A: Probability

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		A2.S.CP.A.2 Understand that two events <i>A</i> and <i>B</i> are independent if the probability of <i>A</i> and <i>B</i> occurring together is the product of their probabilities, and use this characterization to determine if they are independent.	Algebra II M4 Lesson 6: Probability Rules
		A2.S.CP.A.3 Know and understand the conditional probability of <i>A</i> given <i>B</i> as $P(A \text{ and } B)/P(B)$, and interpret independence of <i>A</i> and <i>B</i> as saying that the conditional probability of <i>A</i> given <i>B</i> is the same as the probability of <i>A</i> , and the conditional probability of <i>B</i> given <i>A</i> is the same as the probability of <i>B</i> .	Algebra II M4 Lesson 4: Calculating Conditional Probabilities and Evaluating Independence Using Two-Way Tables Algebra II M4 Lesson 6: Probability Rules
		A2.S.CP.A.4 Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations.	Algebra II M4 Lessons 3–4: Calculating Conditional Probabilities and Evaluating Independence Using Two-Way Tables

Conceptual Category	Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
		Cluster: Use the rules of probability to compute probabilities of compound events in a uniform probability model.	
		A2.S.CP.B.5 Find the conditional probability of <i>A</i> given <i>B</i> as the fraction of <i>B</i> 's outcomes that also belong to <i>A</i> and interpret the answer in terms of the model.	Algebra II M4 Lessons 3–4: Calculating Conditional Probabilities and Evaluating Independence Using Two-Way Tables
		A2.S.CP.B.6 Know and apply the Addition Rule, P(A or B) = P(A) + P(B) - P(A and B), and interpret the answer in terms of the model.	Algebra II M4 Lesson 7: Probability Rules